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Code No. : 14701

**VASAVI COLLEGE OF ENGINEERING (AUTONOMOUS), HYDERABAD**

Accredited by NAAC with A++ Grade

**B.E. (CBCS) IV-Semester Bridge Course Examinations, August-2022**

**Matrix theory and Vector Calculus**

(Common to Civil, Mechanical)

Time: 3 hours

Max. Marks: 50

*Note: Answer all questions from Part-A and any FIVE from Part-B*

**Part-A (10×2 = 20 Marks)**

Q. No.	Stem of the question	M	L	CO	PO
1.	Find the second derivative of $x^2 \sin x$	2	2	1	1,12
2.	Evaluate $\int e^x x dx$	2	1	1	1,12
3.	Define Scalar point function and Gradient.	2	1	2	1,12
4.	Find the divergence of $\vec{F} = (y+z)\vec{i} + (z+x)\vec{j} + (x+y)\vec{k}$	2	2	2	1,12
5.	State Green's theorem in the plane.	2	1	3	1,12
6.	Evaluate $\int_0^1 \int_0^2 xy dy dx$	2	2	3	1,12
7.	Write any two elementary row operations.	2	1	4	1,12
8.	Write any two properties of Eigen values.	2	1	4	1,12
9.	If $z = \cos xy$ then find total derivative of z.	2	2	1	1,12
10.	Define Curl of a vector point function.	2	1	2	1,12
<b>Part-B (5×6 = 30 Marks)</b>					
11.	If $Z = e^{ax+by} \cdot f(ax-by)$ , then Prove that $b \frac{\partial z}{\partial x} + a \frac{\partial z}{\partial y} = 2abz$	6	3	1	1,12
12. a)	Find the Directional derivative of $\phi = x^3 + y^3 + 3xyz$ at (1,1,1) in the direction of the vector $\vec{i} + 2\vec{j} + \vec{k}$ .	4	3	2	1,12
b)	For what value of "β" vector $\vec{F} = (x+3y)\vec{i} + (y-2z)\vec{j} + (x+\beta z)\vec{k}$ is solenoidal vector.	2	1	2	1,12
13.	Evaluate by Stoke's theorem $\int_c \vec{F} \cdot d\vec{r}$ where $\vec{F} = y^2\vec{i} + xy\vec{j} - xz\vec{k}$ . and c is boundary of hemi sphere $x^2 + y^2 + z^2 = a^2$ and $z \geq 0$	6	3	3	1,12
14.	Find Eigen values and Eigen vectors of the matrix $\begin{bmatrix} 4 & 2 & -2 \\ -5 & 3 & 2 \\ -2 & 4 & 1 \end{bmatrix}$	6	3	4	1,12
15. a)	By using implicit differentiation Find $\frac{dy}{dx}$ given that $x^3 + y^3 + 3xy - 1 = 0$	3	2	1	1,12

b)	Find the angle between the surfaces $x^2 + y^2 + z^2 - xy = 1$ and $x^2y + y^2z + z = 1$ at the point $(1, 1, 0)$ .	3	3	2	1,12
16. a)	Evaluate by Green's theorem $\int_c (x^2 - 2xy)dx + (x^2y + 3)dy$ Where $c$ is boundary by $y = x^2$ and $y = x$ .	3	3	3	1,12
b)	Solve the system $x + 2y - z = 1, x + y + 2z = 9, 2x + y - z = 2$ .	3	2	4	1,12
17.	Answer any <i>two</i> of the following:				
a)	Evaluate $\int e^{\sin x} \sin 2x dx$	3	2	1	1,12
b)	If $\vec{F} = y^2\vec{i} + xy\vec{j} - xz\vec{k}$ , then find curl of $\vec{F}$ .	3	2	2	1,12
c)	Evaluate $\int_0^a \int_0^x e^{x+y} dy dx$	3	2	3	1,12

i)	Blooms Taxonomy Level - 1	21.55%
ii)	Blooms Taxonomy Level - 2	35.38%
iii)	Blooms Taxonomy Level - 3 & 4	43.07%

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